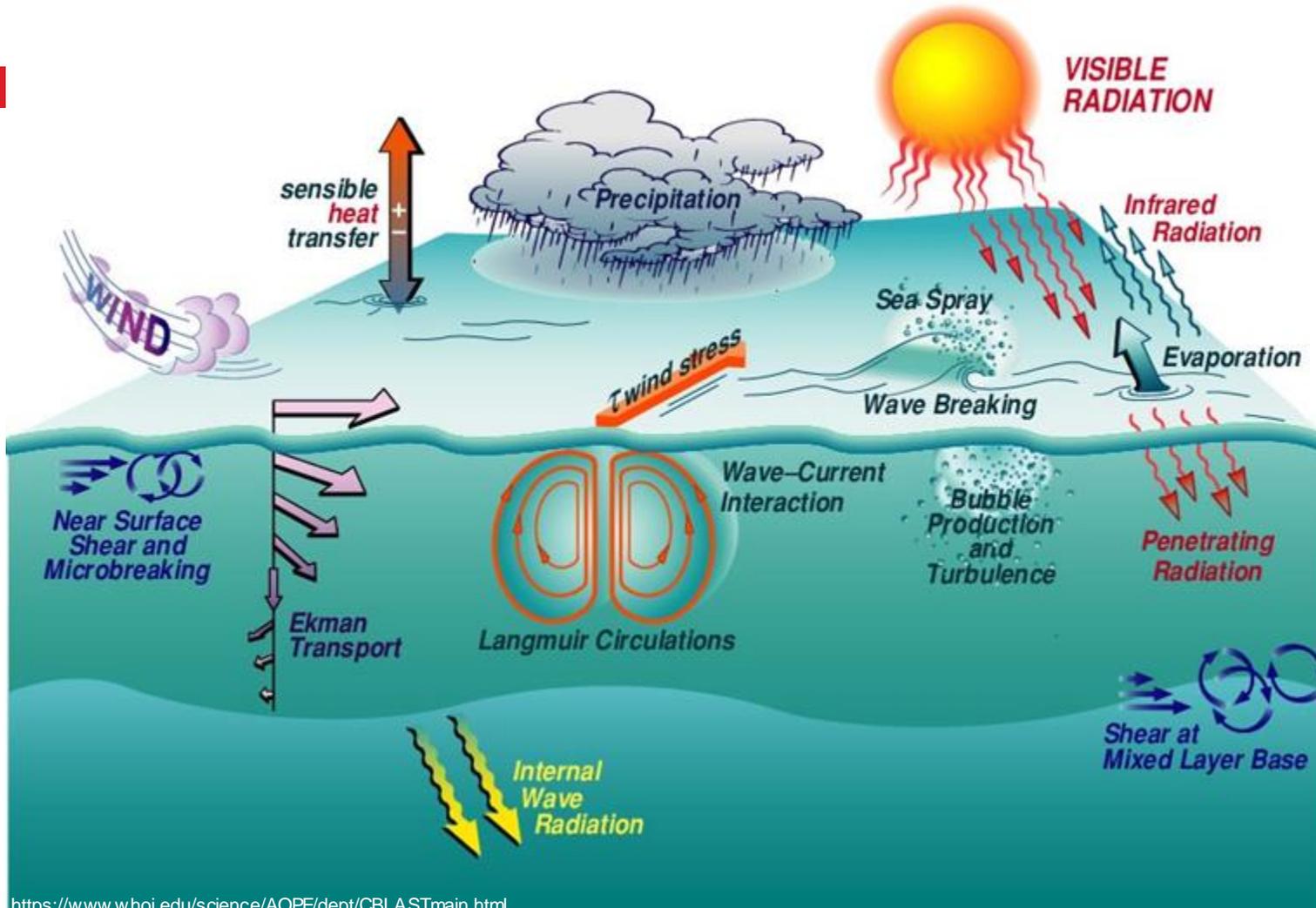


The wave-mediated ocean-atmosphere system

Øyvind Breivik, Ana Carrasco, Alfatih Ali, Mika Malila, Trygve Halsne, Maria Bjørnestad, Gaute Hope, Torunn Seldal, Jean Rabault & Tor Nordam (SINTEF/NTNU)



Small-scale mixing processes in the upper ocean

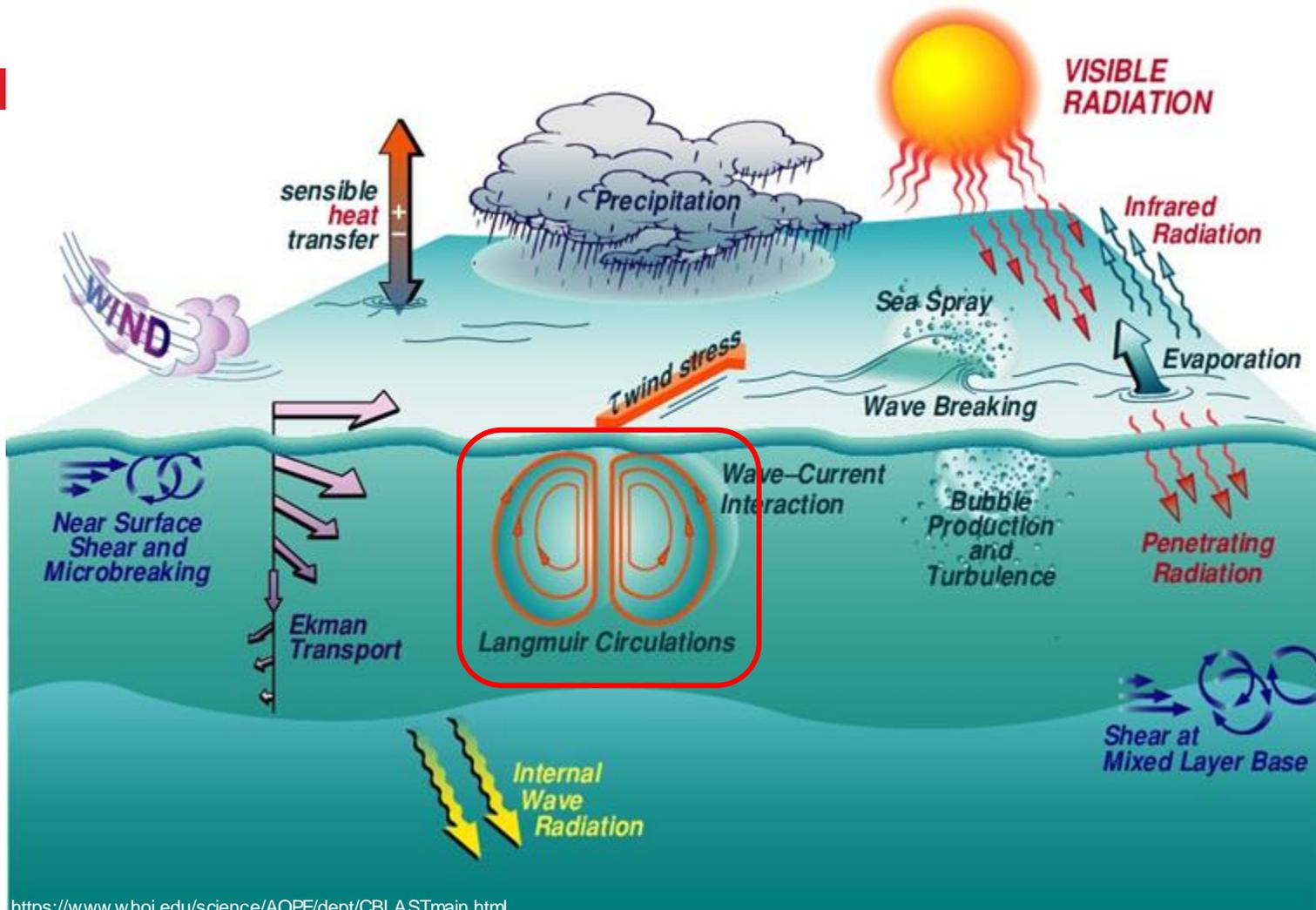


Turbulent kinetic energy budget

$$\frac{De}{Dt} = \underbrace{-\overline{u'_h w'}}_1 \cdot \frac{\partial \mathbf{u}_h}{\partial z} - \underbrace{\overline{u'_h w'}}_2 \cdot \frac{\partial \mathbf{u}_s}{\partial z} + \underbrace{\overline{w' b'}}_3 - \underbrace{\frac{\partial}{\partial z} \left\{ \overline{w' u'_i u'_i} + \frac{1}{\rho_0} \overline{w' p'} \right\}}_4 - \underbrace{\epsilon}_5$$

1. Shear production
2. Stokes production
3. Buoyant production
4. Turbulent transport
5. Dissipation

Wave-driven mixing processes in the upper ocean



<https://www.whoi.edu/science/AOPF/dept/CBL-ASTmain.html>

Turbulent kinetic energy budget

$$\frac{De}{Dt} = \underbrace{-\overline{u'_h w'}}_1 \cdot \frac{\partial \overline{u_h}}{\partial z} + \underbrace{\overline{u'_h w'}}_2 \cdot \frac{\partial \overline{u_s}}{\partial z} + \underbrace{\overline{w' b'}}_3 - \underbrace{\frac{\partial}{\partial z} \left\{ \overline{w' u'_i u'_i} + \frac{1}{\rho_0} \overline{w' p'} \right\}}_4 - \underbrace{\epsilon}_5$$

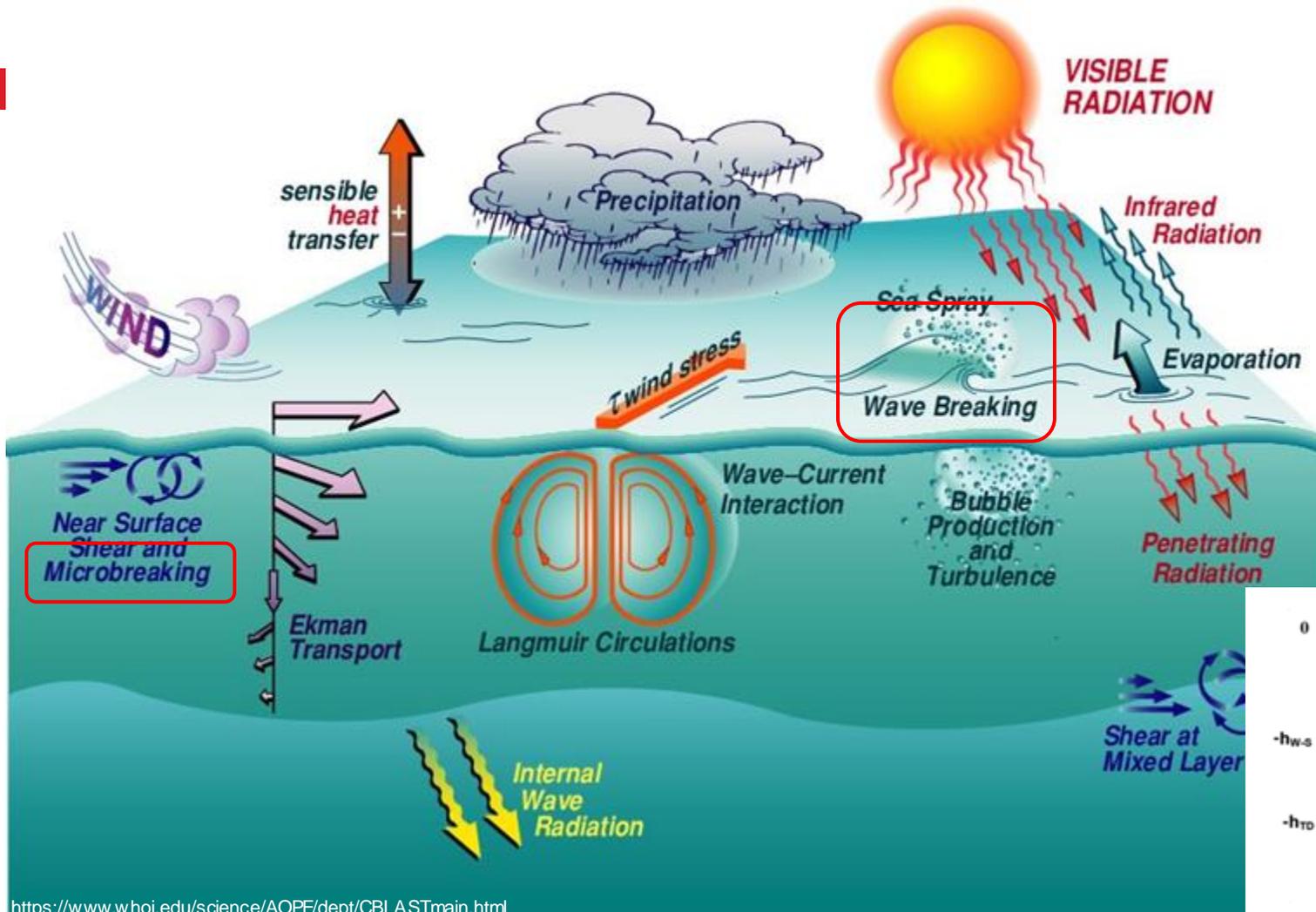
1. Shear production
2. **Stokes production (wave-averaged)**
3. Buoyant production
4. Turbulent transport
5. Dissipation

Langmuir turbulence



- Occurs due to interaction between waves (Stokes drift) and vorticity
- Enhances mixing in OSBL
- Transports properties vertically across OSBL
- May deepen mixed layer depth

Wave-driven mixing processes in the upper ocean



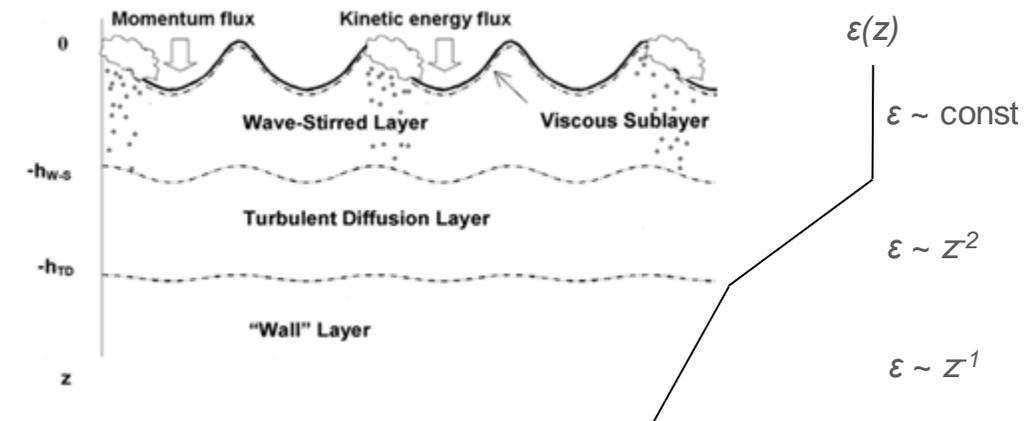
<https://www.whoi.edu/science/AOPF/dept/CBL-ASTmain.html>

Turbulent kinetic energy budget

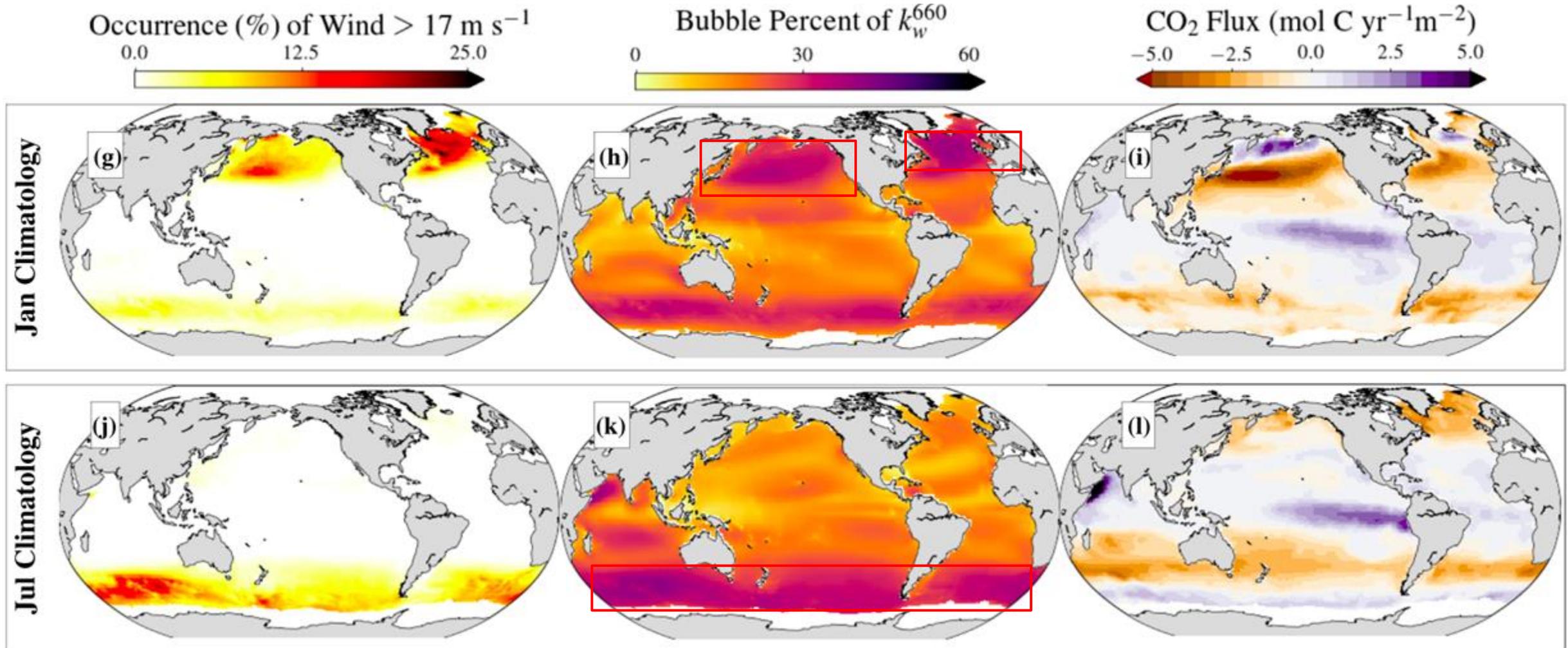
$$\frac{De}{Dt} = \underbrace{-\overline{u'_h w'}}_1 \cdot \frac{\partial \overline{u}_h}{\partial z} - \underbrace{\overline{u'_h w'}}_2 \cdot \frac{\partial \overline{u}_s}{\partial z} + \underbrace{\overline{w' b'}}_3 - \underbrace{\frac{\partial}{\partial z} \left\{ \overline{w' u'_i u'_i} + \frac{1}{\rho_0} \overline{w' p'} \right\}}_4 - \underbrace{\epsilon}_5$$

1. Shear production
2. Stokes production
3. Buoyant production
4. Turbulent transport
5. **Dissipation**

Enhanced dissipation due to wave breaking (Craig and Banner, 1994)



The bubble-mediated CO₂ flux



~40% of the net global air-sea CO₂ flux is mediated by bubbles

Bubble contribution has significant spatial variability

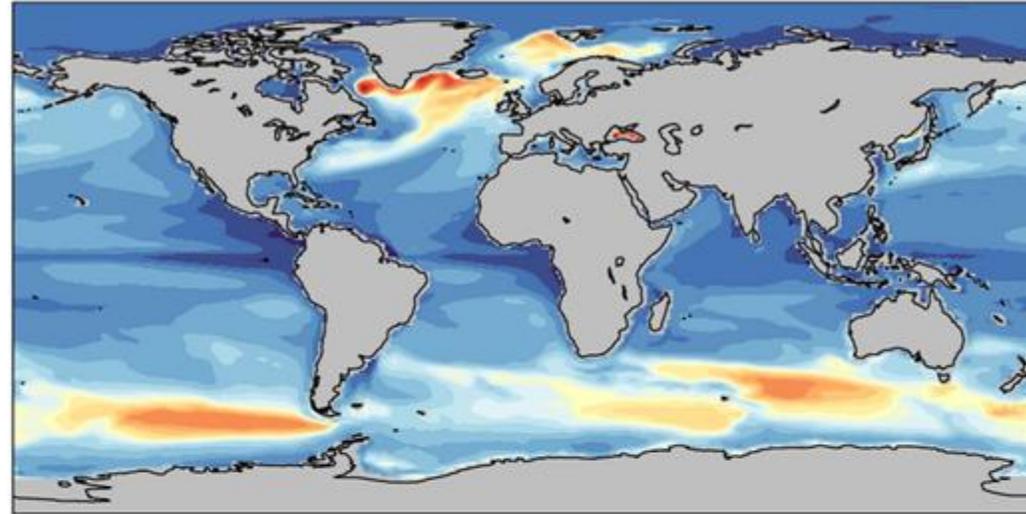
Langmuir turbulence parameterised in climate models

6

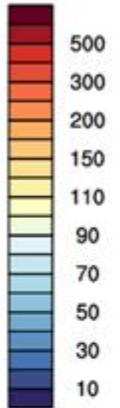
The mixed layer depth of the global ocean component of the Norwegian Earth System model (NorESM) - too thin

AA_NOIIAJRA20TR_TL319_tn14_20230630 (yrs 42-61)

Mixed layer depth mean= 51.50 m

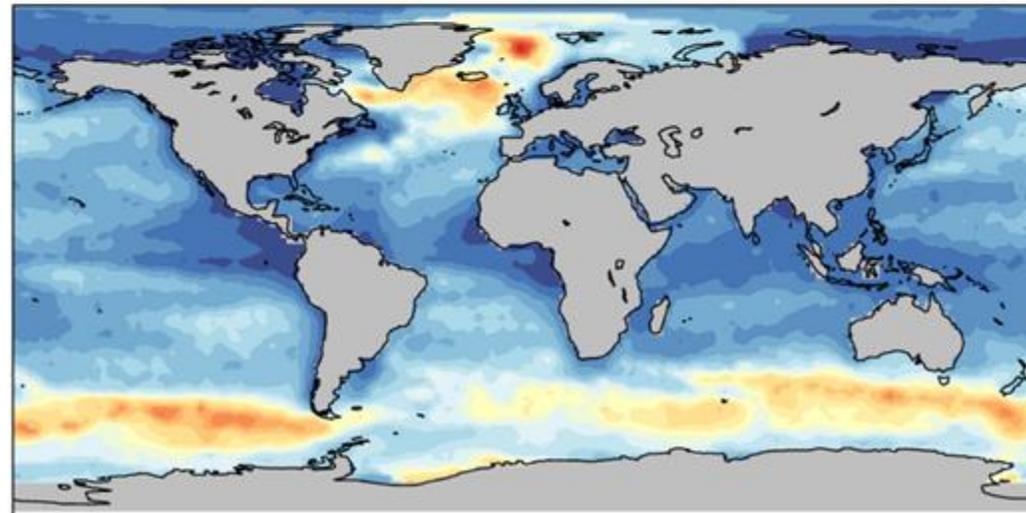


Min = 3.49 Max = 841.72

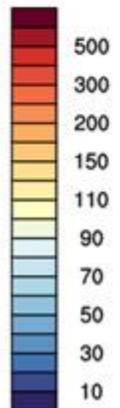


de Boyer Montegut et al. (2004)

Mixed layer depth mean= 57.22 m



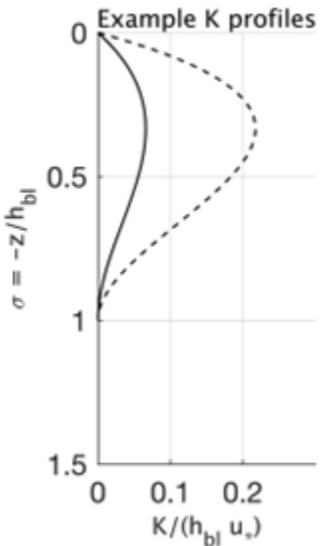
Min = 10.14 Max = 500.93



Langmuir turbulence parameterised in climate models

7

Add a bit of mixing based on the Langmuir enhancement factor in the KPP scheme ...



See Alfatih Ali's poster

Langmuir mixing parameterization in KPP

- In the KPP scheme, the turbulent eddy diffusivity of a property X within the ocean surface boundary layer $0 < z < h$ is parameterized as

$$K_x(z, t) = h(t) w_x(z/h, t) G(z/h).$$

- The ocean boundary layer depth h is determined as the shallowest depth at which the bulk Richardson number $Ri_b(z)$ rises above a critical value Ri_c :

$$Ri_b(z) = \frac{(B_r - B(z))|z|}{|\mathbf{u}_r - \mathbf{u}(z)|^2 + V_t^2(z)}.$$

- LT effects are parameterized following McWilliams and Sullivan (2000) through an enhancement factor $\mathcal{E}(La_t)$ applied to the turbulent velocity scale as

$$w_x = (\kappa u_* / \phi) \mathcal{E}(La_t) \quad \text{where} \quad \mathcal{E}(La_t) = [1 + C_w / La_t^{2\alpha}]^{1/\alpha}$$

- The LT-enhanced unresolved turbulence shear: $V_{tL}^2(z) = \frac{C_v N(z) (\kappa u_* / \phi) \mathcal{E}(La_t) |z|}{Ri_c \kappa^2} \left(\frac{-\beta_T}{\epsilon} \right)^{\frac{1}{2}}$

Table: Description of the four experiments where CNTL is the control run without wave effects. VR12PAR refers to the experiment where Stokes drift profile is parameterized from wind, while VR12 and LF17 experiments are coupled with WAVEWATCH III.

Parameterization	Exp.	Enhancement factor $\mathcal{E}(La_{SL})$	Unresolved shear	Wave coupling
Large et al. (1994)	CNTL	1	V_t^2	No coupling
Van Roekel et al. (2012)	VR12	$\sqrt{1 + (1.5La_{SL})^{-2} + (5.4La_{SL})^{-4}}$	V_t^2	WAVEWATCH III
Li et al. (2017)	VR12PAR	same as VR12	same as VR12	Parameterized Stokes profile
Li and Fox-Kemper (2017)	LF17	same as VR12	V_{tL}^2	WAVEWATCH III

- LT enhancement of the buoyancy entrainment at the base of the boundary layer (Li and Fox-Kemper, 2017):

The unresolved turbulence shear is modified: $V_{tL}^2(z) = \frac{C_v N(z) w_s(z) |z|}{Ri_c} \left[\frac{-\overline{w'b'_c} h}{w_s(z)^3} \right]^{\frac{1}{2}}$

Enhanced entrainment buoyancy flux: $-\overline{w'b'_c} = \frac{u_*^3}{h} \left(0.17 + 0.083 La_{SL}^{-2} - 0.15 \frac{h}{\kappa L} \right)$

Langmuir turbulence parameterised in climate models

8

Add a bit of mixing based on the Langmuir enhancement factor in the KPP scheme ...

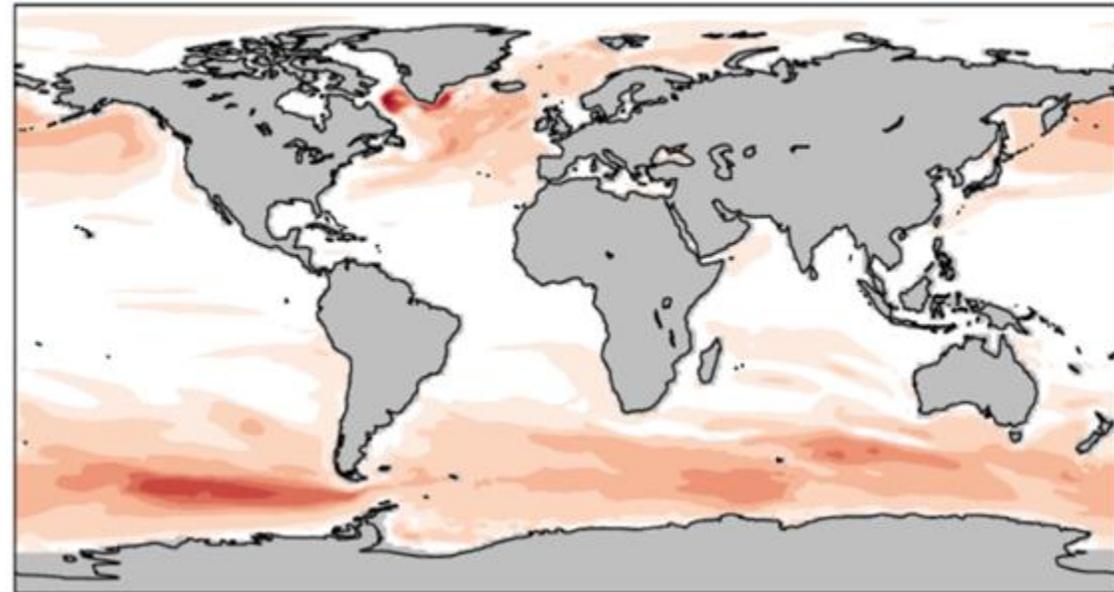
and things improve ...

MLD: LF17 - CNTL

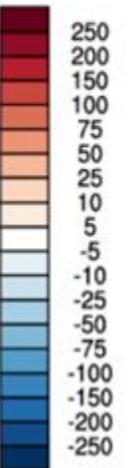
mean = 10.41

rmse = 18.39

m



Min = -45.53 Max = 252.5



Langmuir turbulence parameterised in climate models

9

Add a bit of mixing based on the Langmuir enhancement factor in the KPP scheme ...

and things improve *on average* ...

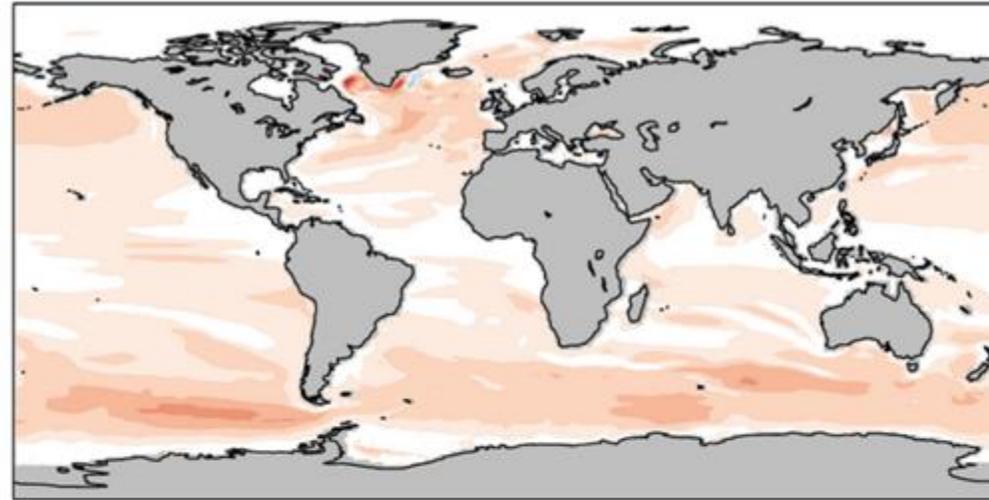
but, do we really need wave models for that?

MLD: VR12PAR - CNTL

mean = 8.72

rmse = 11.76

m



Min = -47.52 Max = 165.45

Stokes drift profile parameterised from local wind

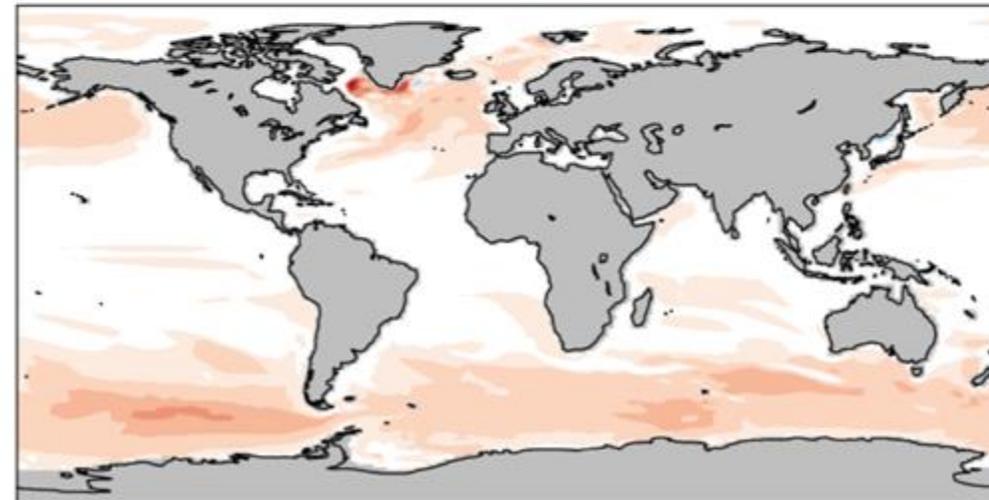
vs

MLD: VR12 - CNTL

mean = 7.16

rmse = 10.88

m



Min = -69.68 Max = 241.80

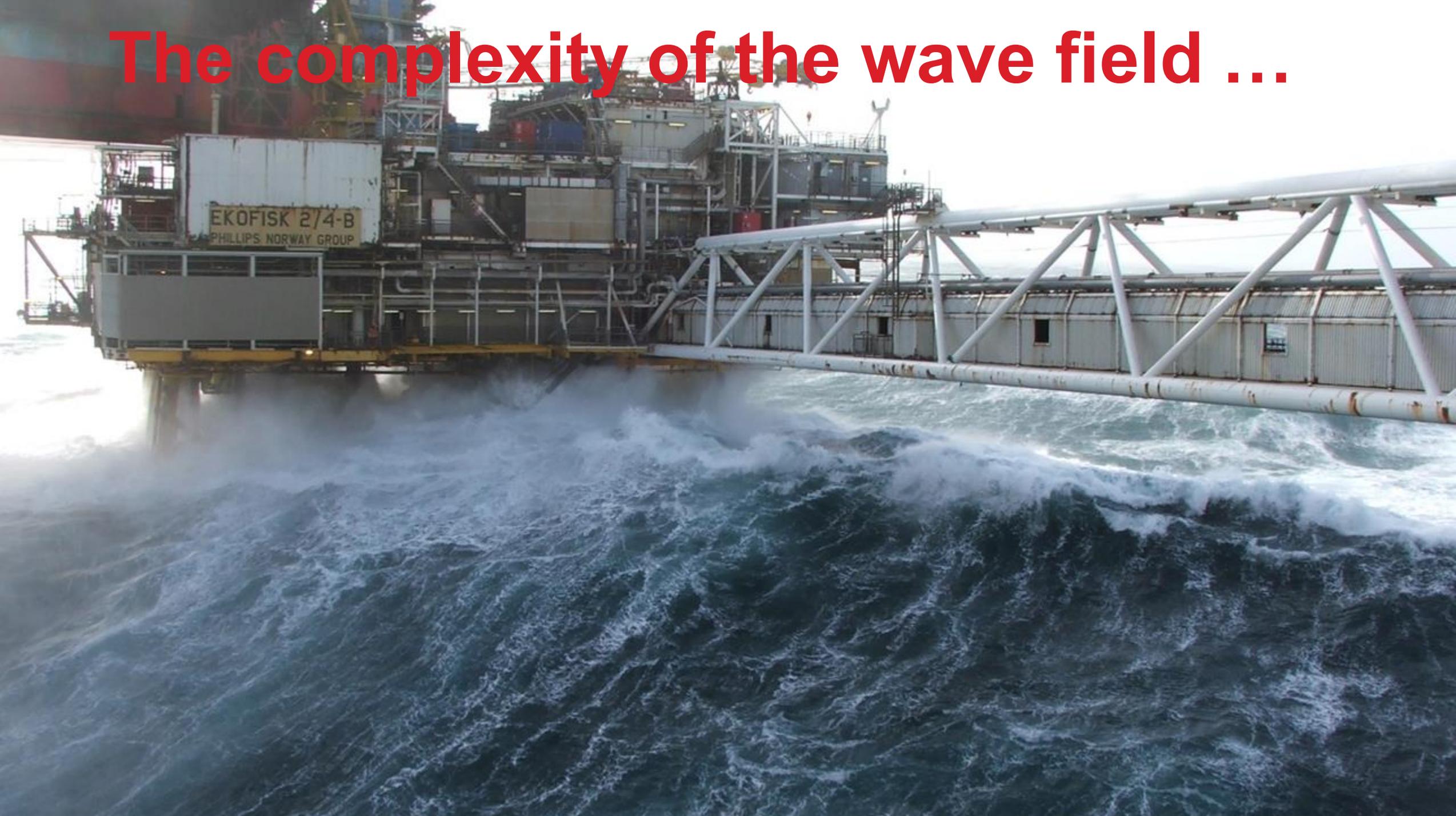
Stokes drift profile from wave model

Intermediate conclusion

10

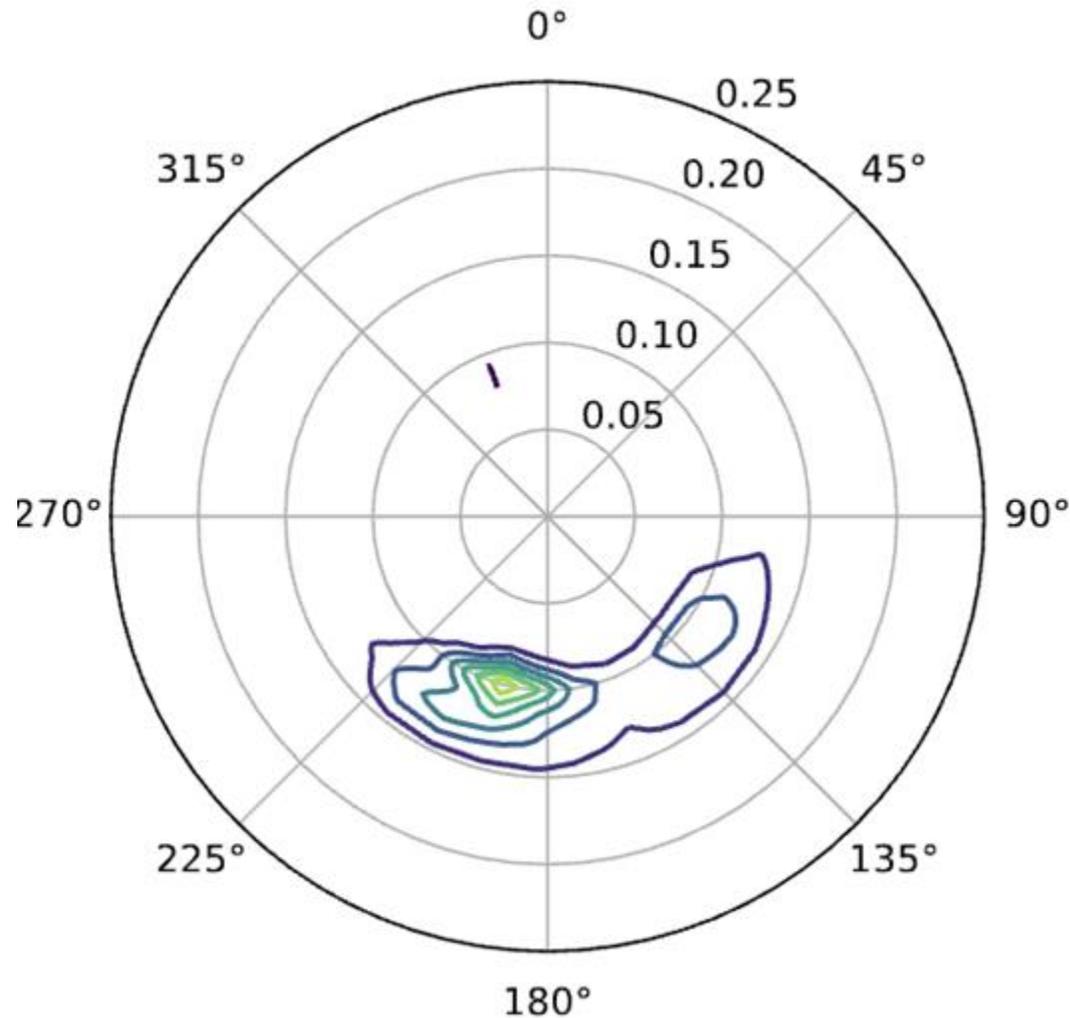
- Wave models are necessary and essential for certain types of coupled systems, like the IFS, because they determine the *evolution* of the weather systems
- But, wave models are necessary to *inform*, but may not be *affordable or necessary* for all sorts of coupled models where only *mean quantities* need to be correct

The complexity of the wave field ...



The complexity of the wave field ...

... reduced to this

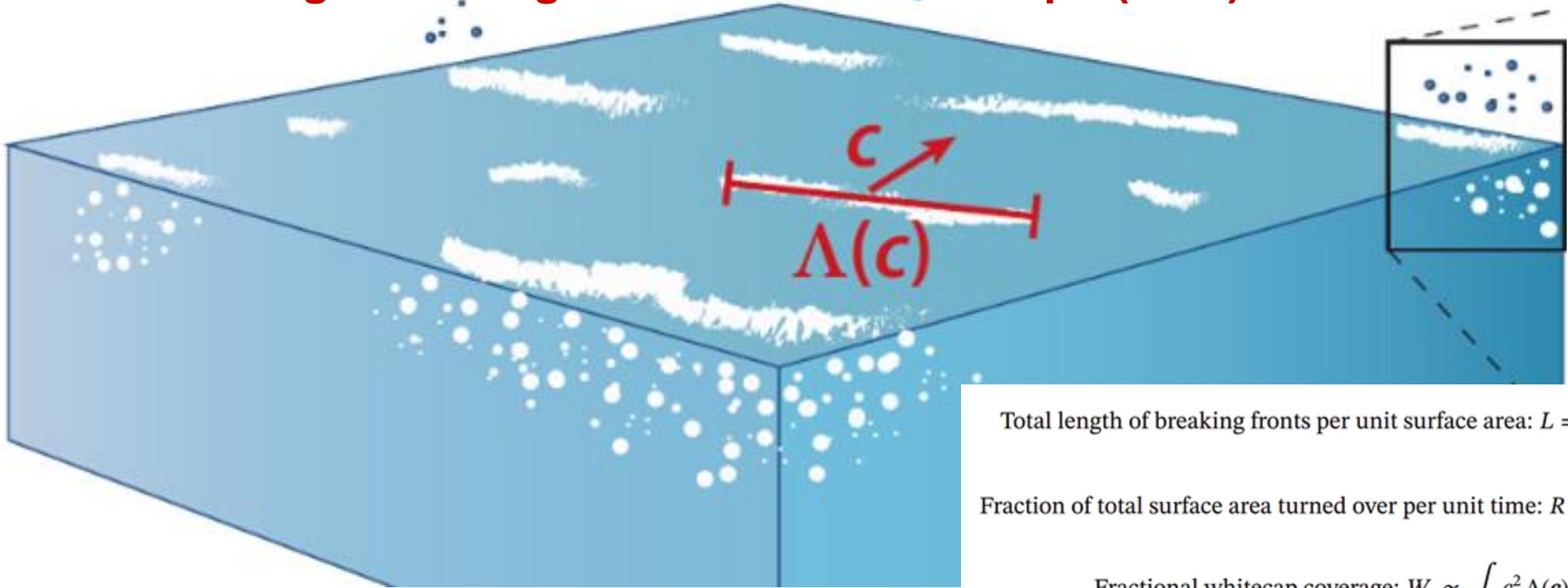


The richness of the wave field ...



- cannot possibly be captured by the two-dimensional spectrum
- can we continue to parameterise the processes responsible for the air-sea interaction the way we have?
- and if so, can we do better by turning to new types of measurements?

The breaking crest length distribution of Phillips (1985)



Total length of breaking fronts per unit surface area: $L = \int \Lambda(\mathbf{c}) d\mathbf{c}$

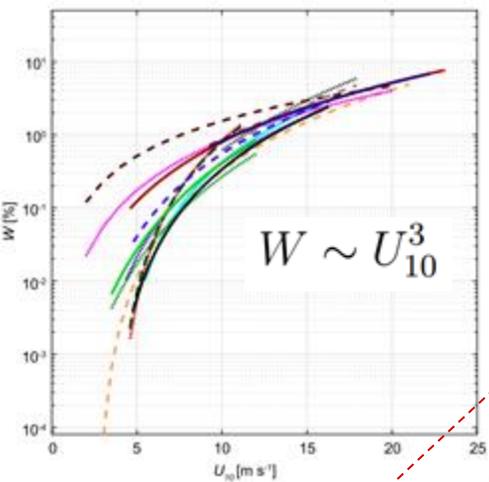
Fraction of total surface area turned over per unit time: $R = \int c \Lambda(\mathbf{c}) d\mathbf{c}$

Fractional whitecap coverage: $W \propto \int c^2 \Lambda(\mathbf{c}) d\mathbf{c}$

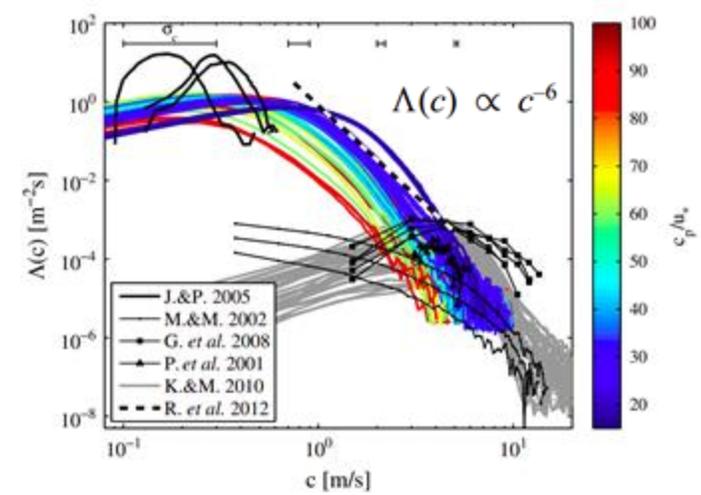
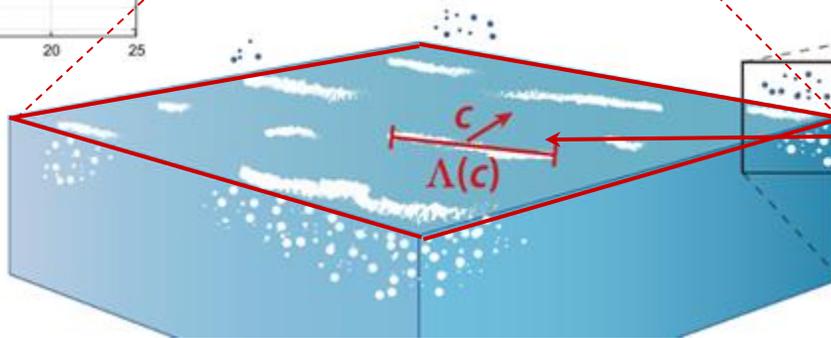
Rate of air entrainment per unit surface area: $V_a \propto \int c^3 \Lambda(\mathbf{c}) d\mathbf{c}$

Momentum flux per unit surface area: $M \propto \int c^4 \Lambda(\mathbf{c}) d\mathbf{c}$

Energy dissipation per unit surface area: $E \propto \int c^5 \Lambda(\mathbf{c}) d\mathbf{c}$



Whitecap coverage



Breaking crest length distribution $\Lambda(c)$
Phillips (1985)

Total length of breaking fronts per unit surface area: $L = \int \Lambda(c)dc$

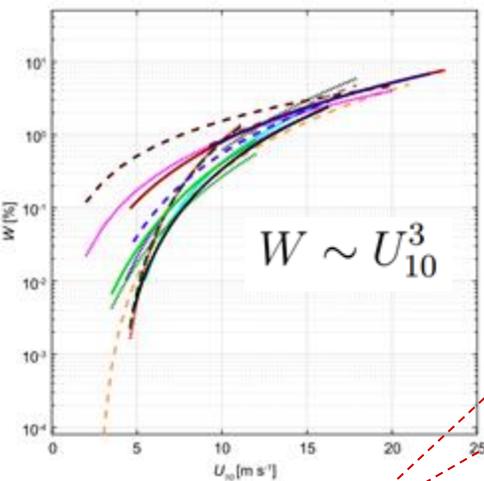
Fraction of total surface area turned over per unit time: $R = \int c\Lambda(c)dc$

Fractional whitecap coverage: $W \propto \int c^2 \Lambda(c)dc$

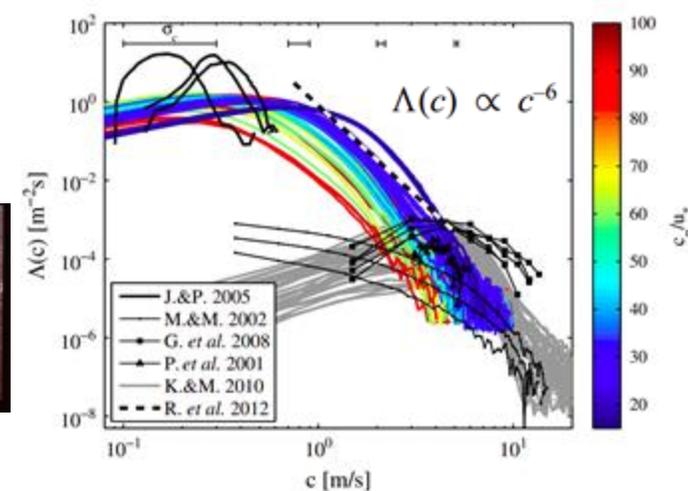
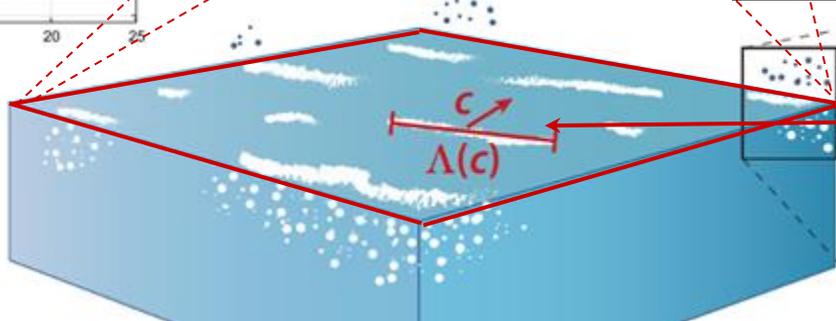
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Whitecap coverage &
Stereo reconstruction



Breaking crest length distribution $\Lambda(c)$
Phillips (1985)

$$\text{Total length of breaking fronts per unit surface area: } L = \int \Lambda(c) dc$$

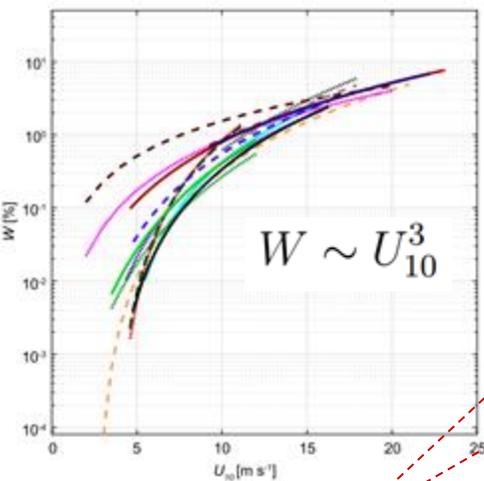
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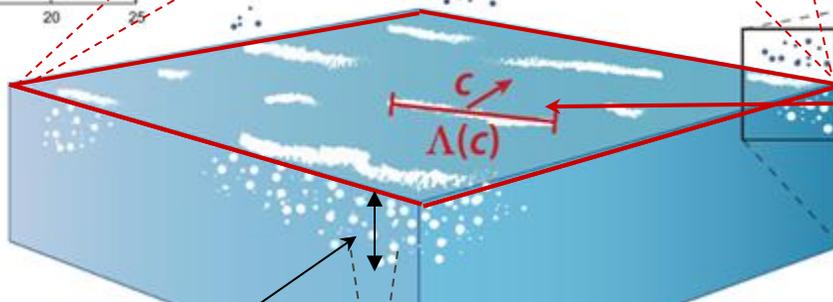
$$\text{Rate of air entrainment per unit surface area: } V_a \propto \int c^3 \Lambda(c) dc$$

$$\text{Momentum flux per unit surface area: } M \propto \int c^4 \Lambda(c) dc$$

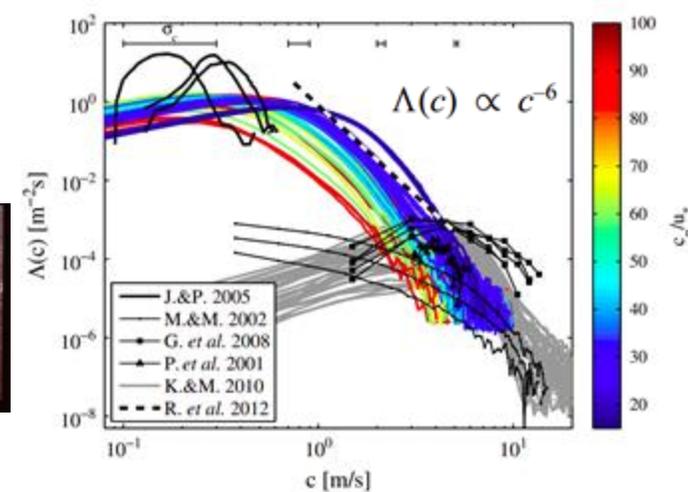
$$\text{Energy dissipation per unit surface area: } E \propto \int c^5 \Lambda(c) dc$$



Whitecap coverage &
Stereo reconstruction



ADCP Bubble plume
depth Z_p



Breaking crest length distribution $\Lambda(c)$
Phillips (1985)

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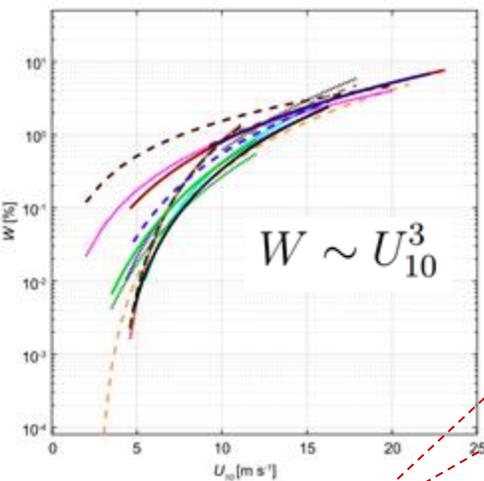
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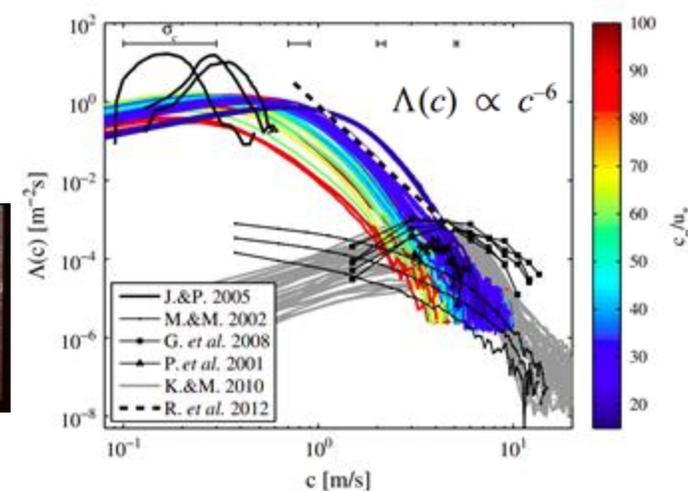
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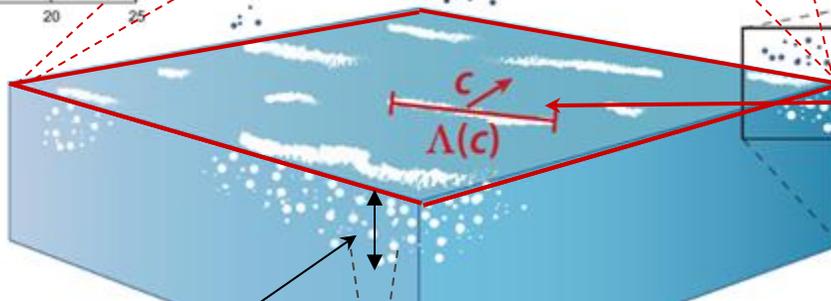
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Whitecap coverage &
Stereo reconstruction



Breaking crest length distribution $\Lambda(c)$
Phillips (1985)



ADCP Bubble plume
depth Z_p



Subsurface camera for
bubble size distribution

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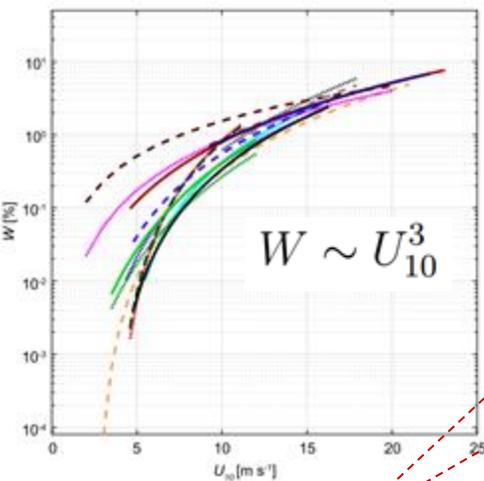
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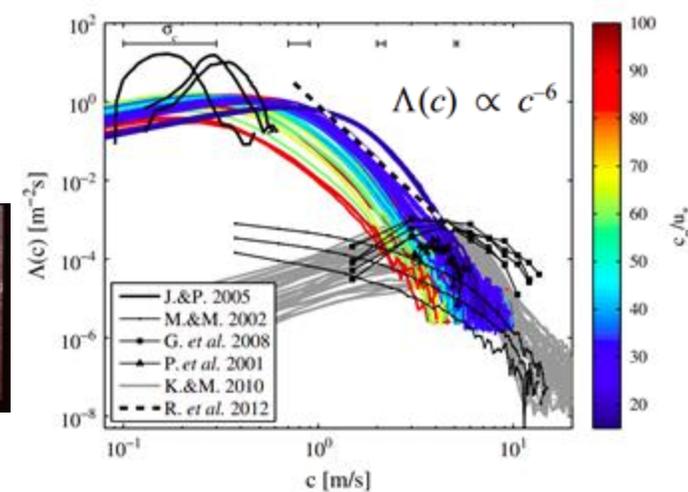
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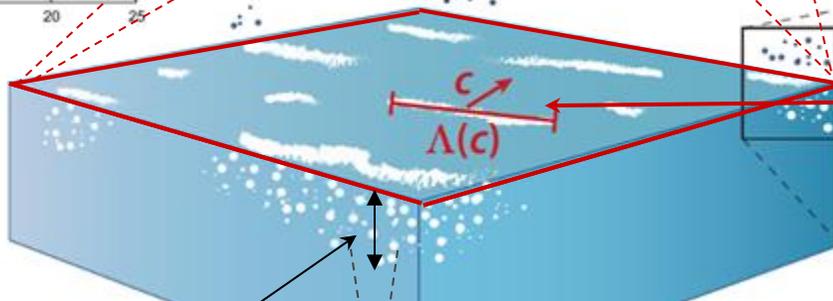
Energy dissipation per unit surface area: $E \propto \int c^5 \Lambda(c)dc$



Whitecap coverage &
Stereo reconstruction



Breaking crest length distribution $\Lambda(c)$
Phillips (1985)



ADCP Bubble plume
depth Z_p



Subsurface camera for
bubble size distribution

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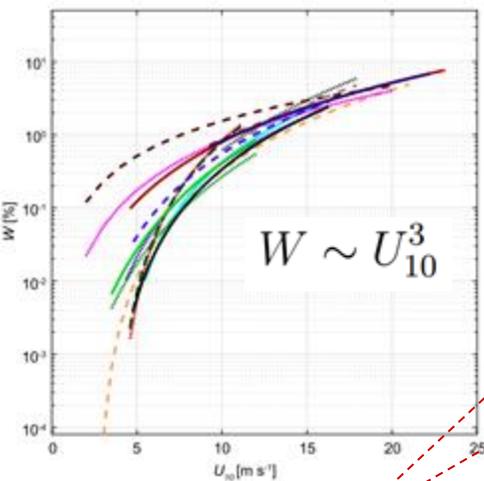
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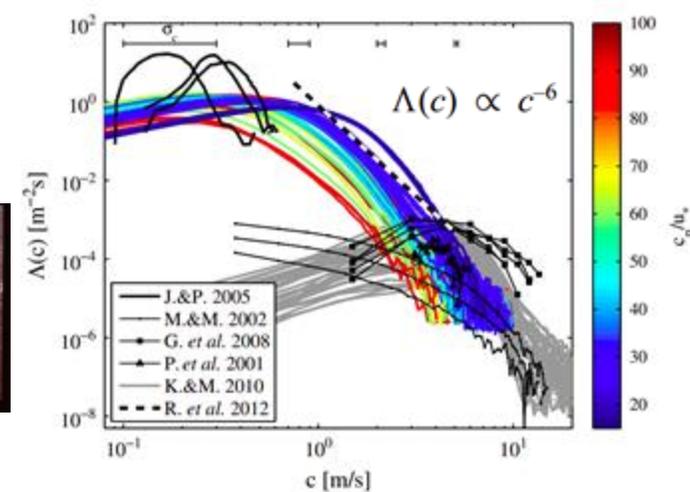
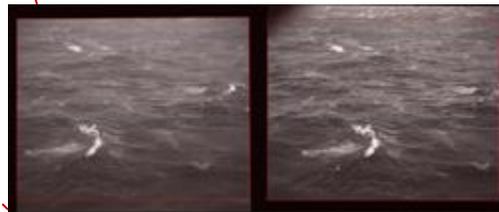
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Whitecap coverage & Stereo reconstruction



Breaking crest length distribution $\Lambda(c)$
Phillips (1985)

Sensor buoy built into a boat fender
interweight 13mm LL chain

Moored miniature buoy

Weigl
12m x 6mm wir
weight and mo

ADCP Bubble plume
depth Z_p



Subsurface camera for
bubble size distribution

Total length of breaking fronts per unit surface area: $L = \int \Lambda(c)dc$

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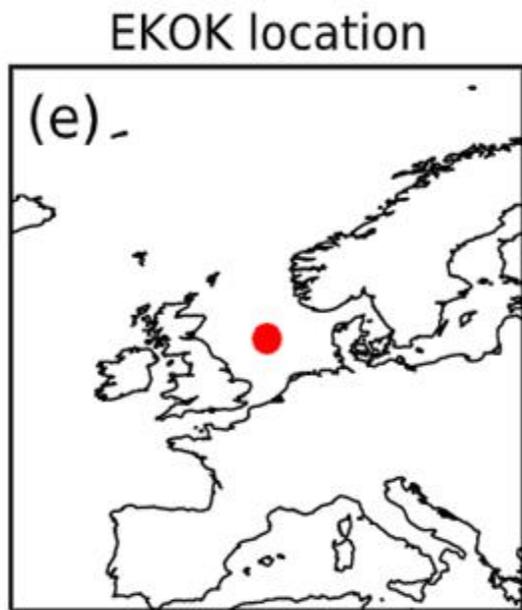
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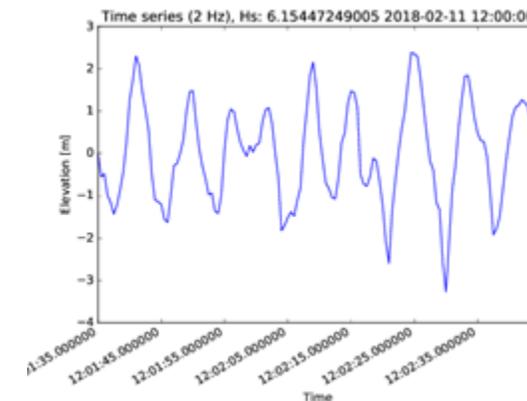
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Ekofisk - an open-ocean wave laboratory since 1980



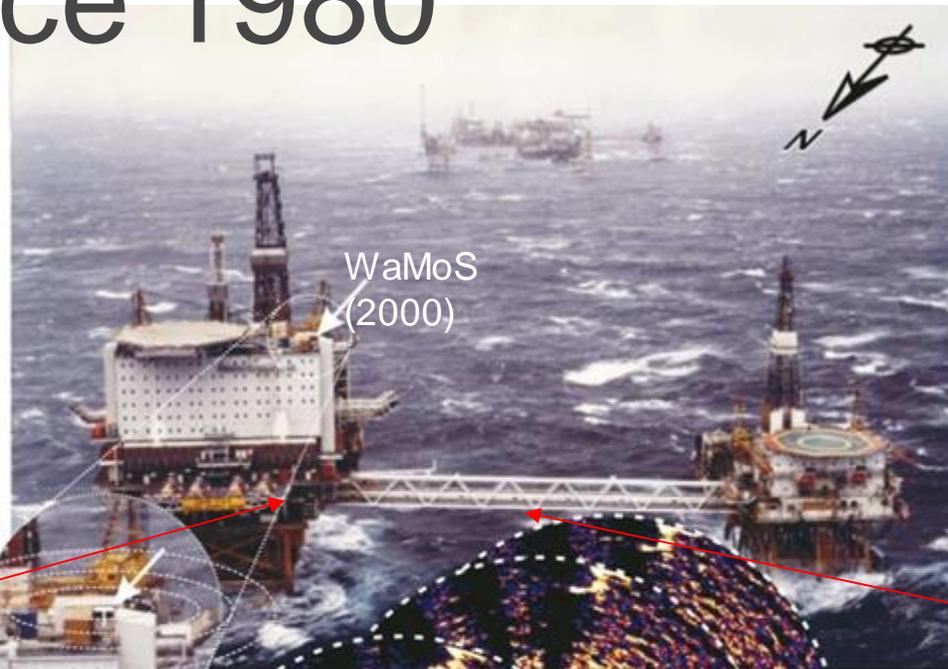
LASAR (2003)



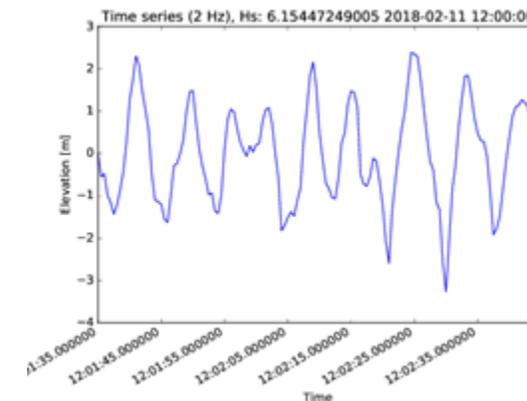
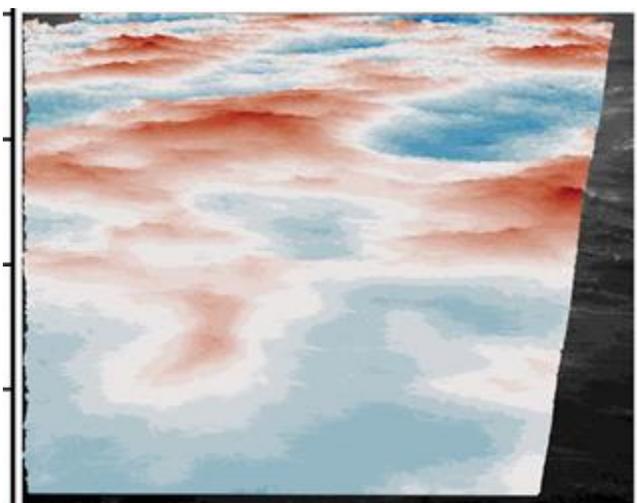
Ekofisk - an open-ocean wave laboratory since 1980



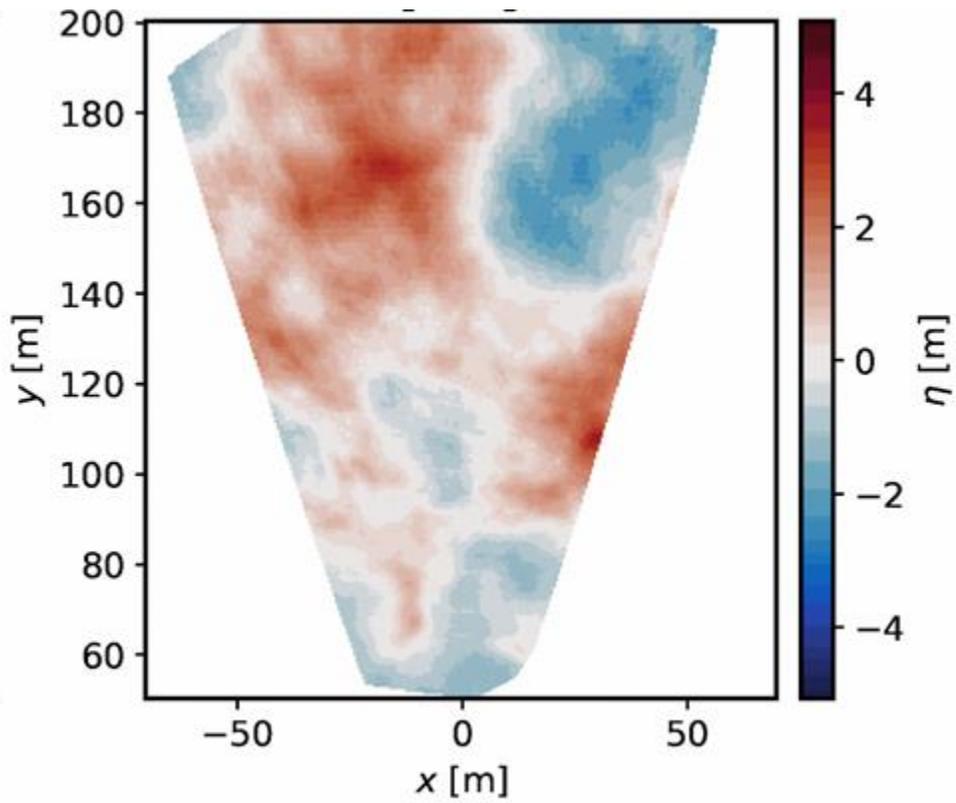
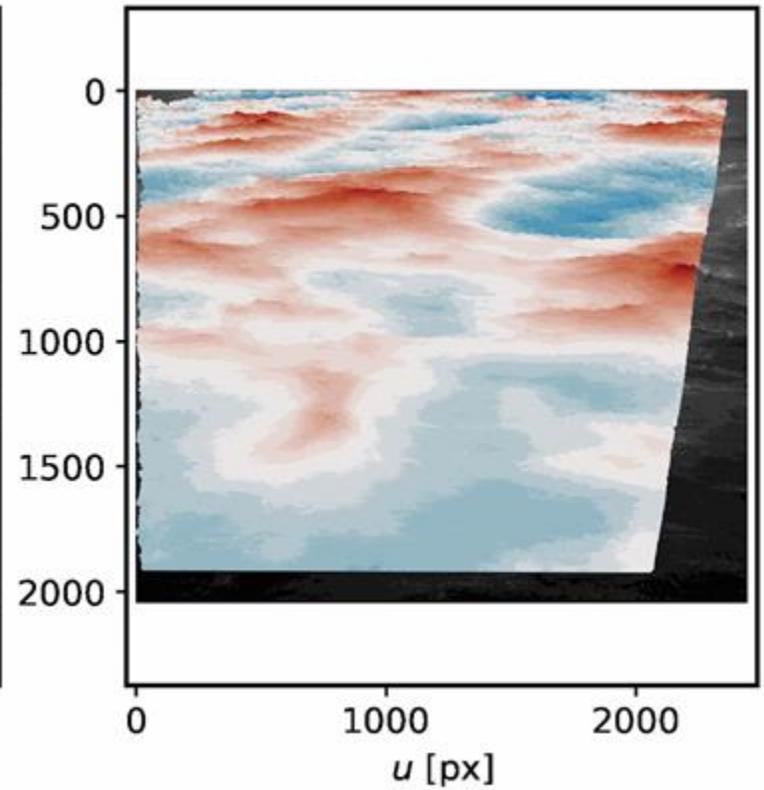
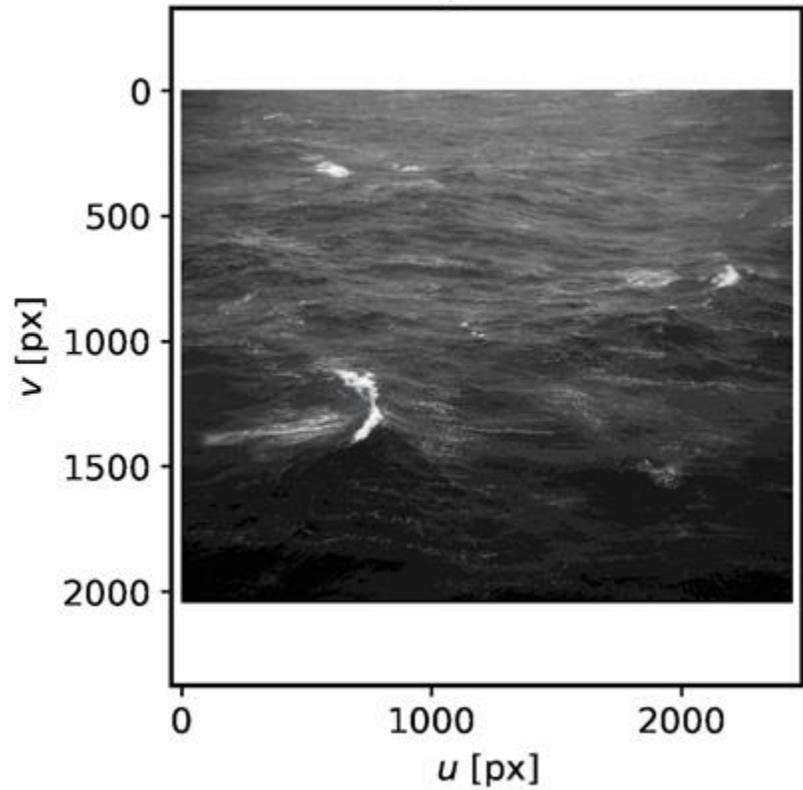
Stereo video (2017)



LASAR (2003)

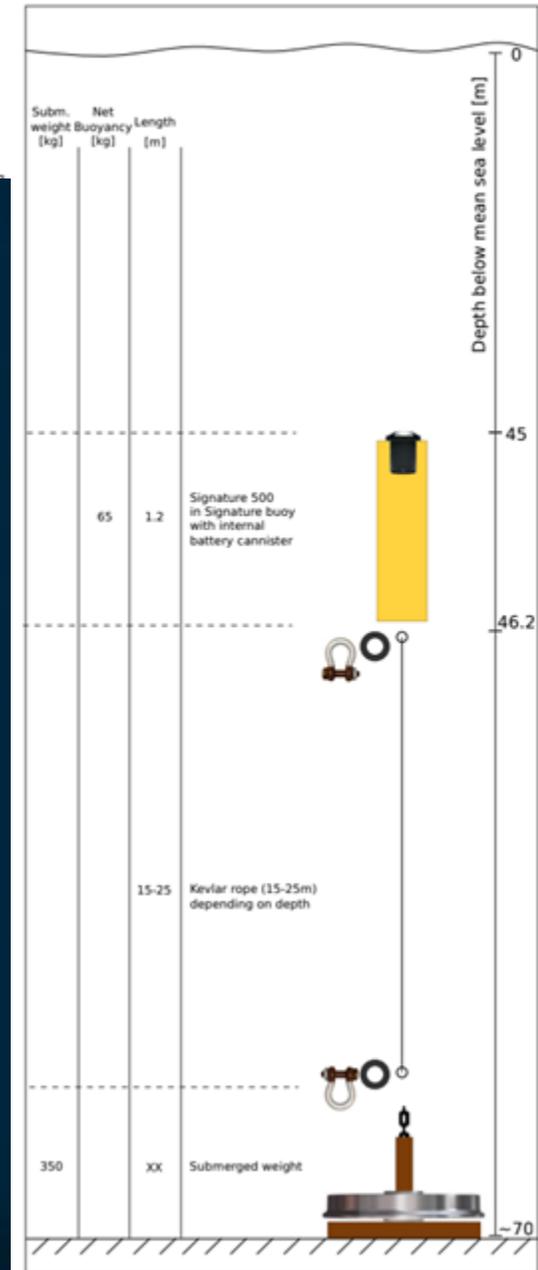


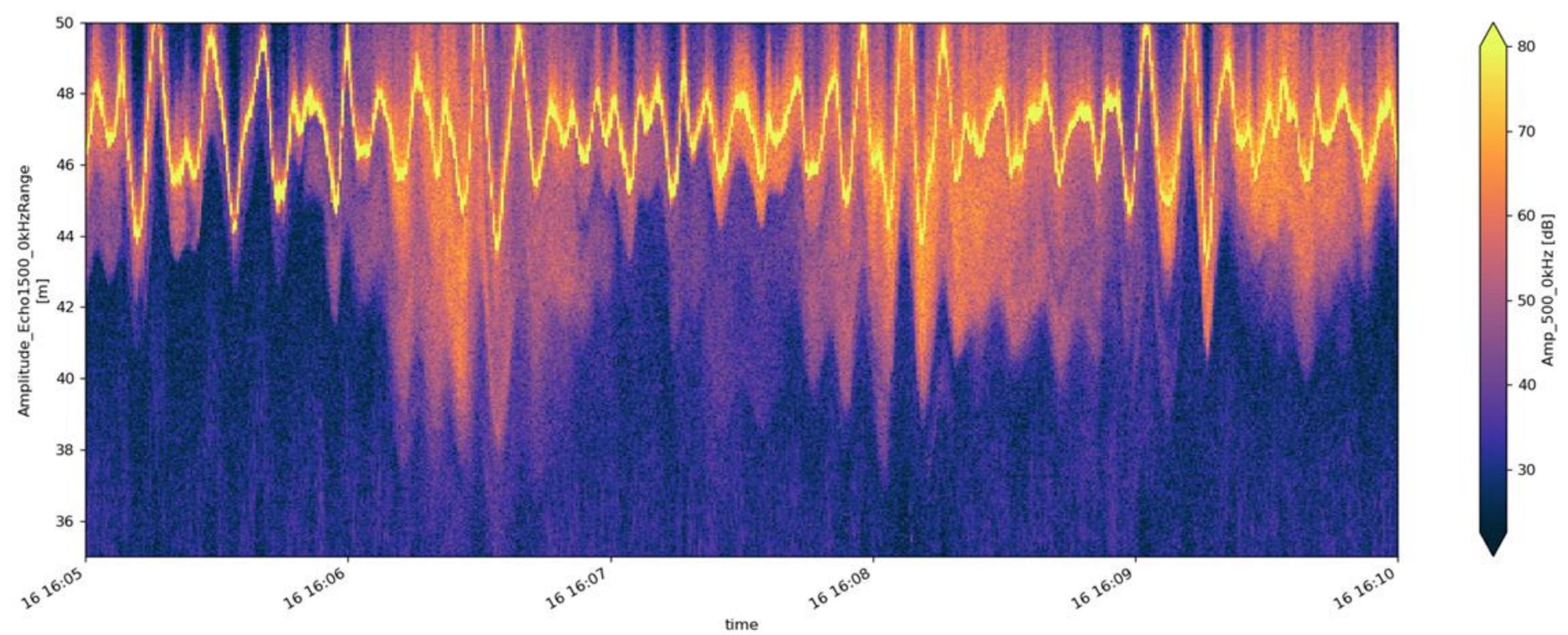
Since 2017: Stereo measurements (5 Hz)



2022: Deployment of ADCP in the stereo camera field of view

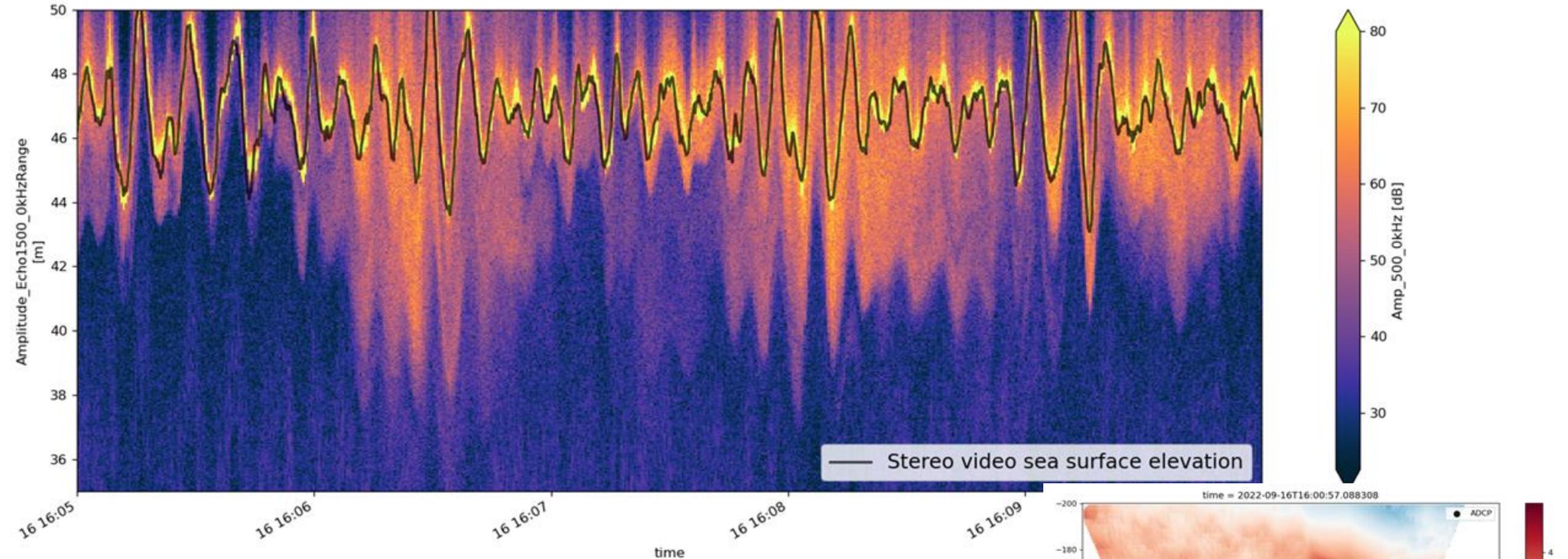
Project name : ADCP EKOF
 Depth : 70 m
 Longitude : N/A
 Latitude : N/A





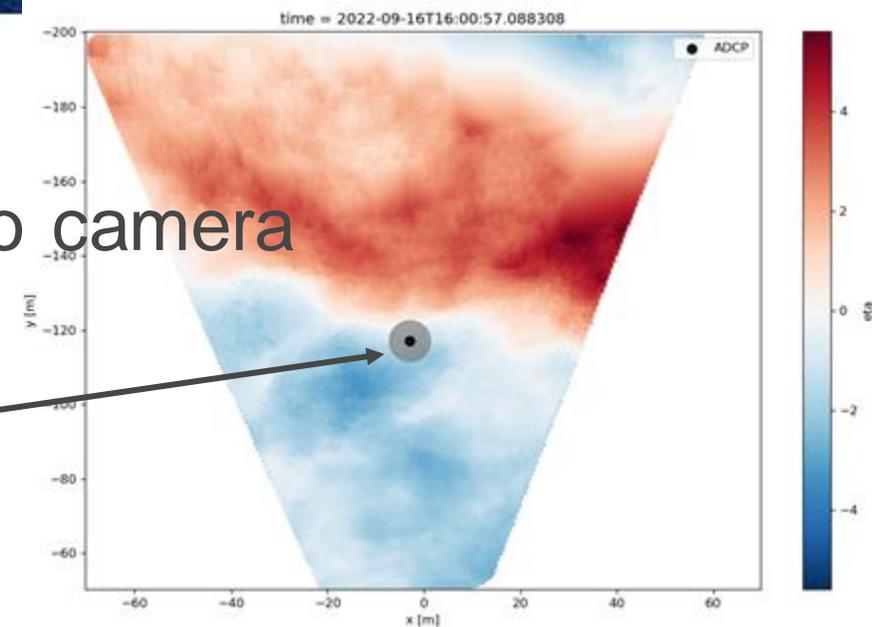
The fifth beam of a Nortek 500 ADCP

- 5 minute time series of raw echosounder image
- Brighter yellow indicates stronger backscatter, bubble plumes clearly visible

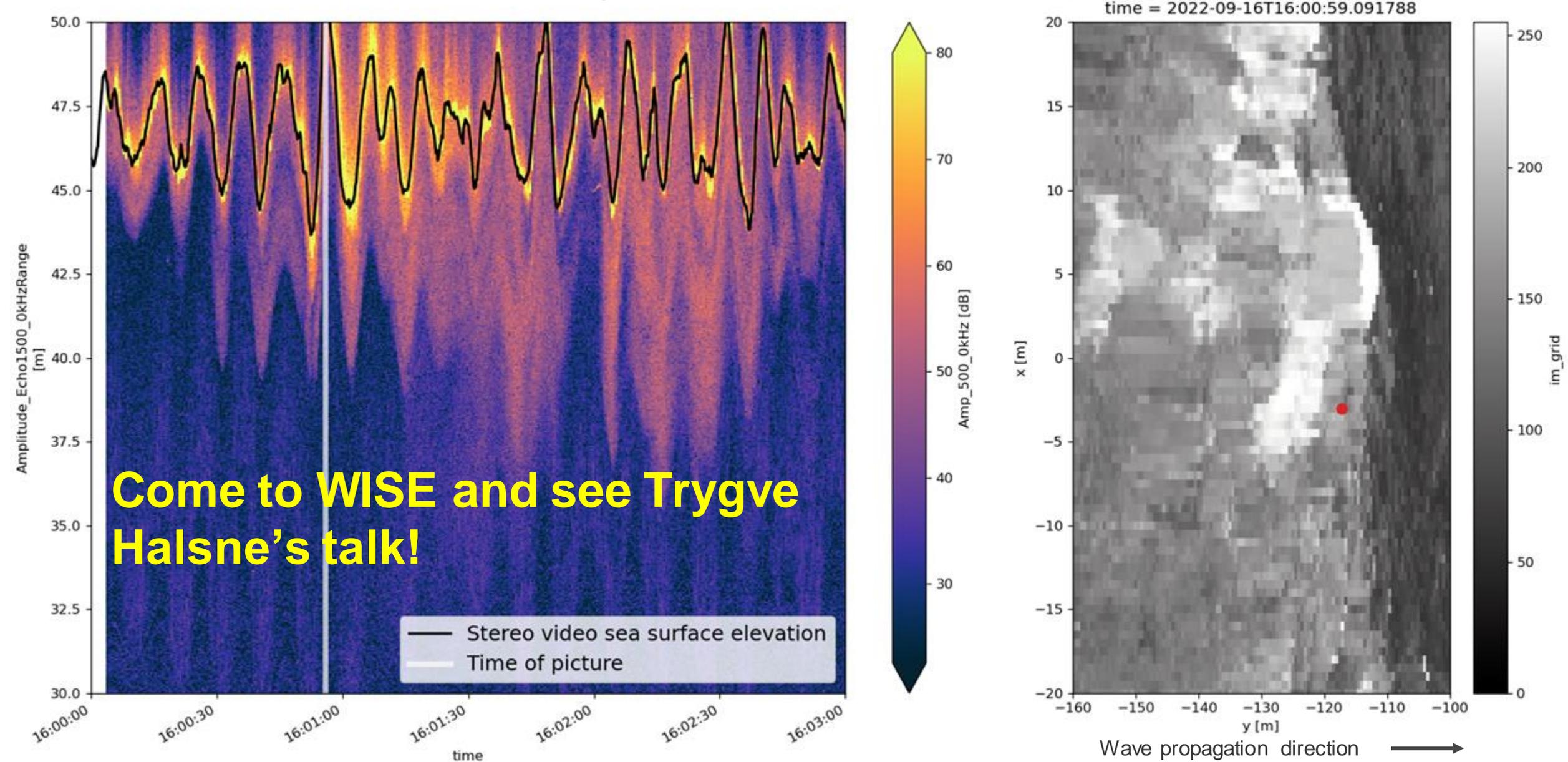


The fifth beam of a Nortek 500 ADCP & a stereo camera

- 5 minute time series of raw echosounder image
- Brighter yellow indicates stronger backscatter
- ADCP located here



Identified wave breaking events in the vicinity of the ADCP



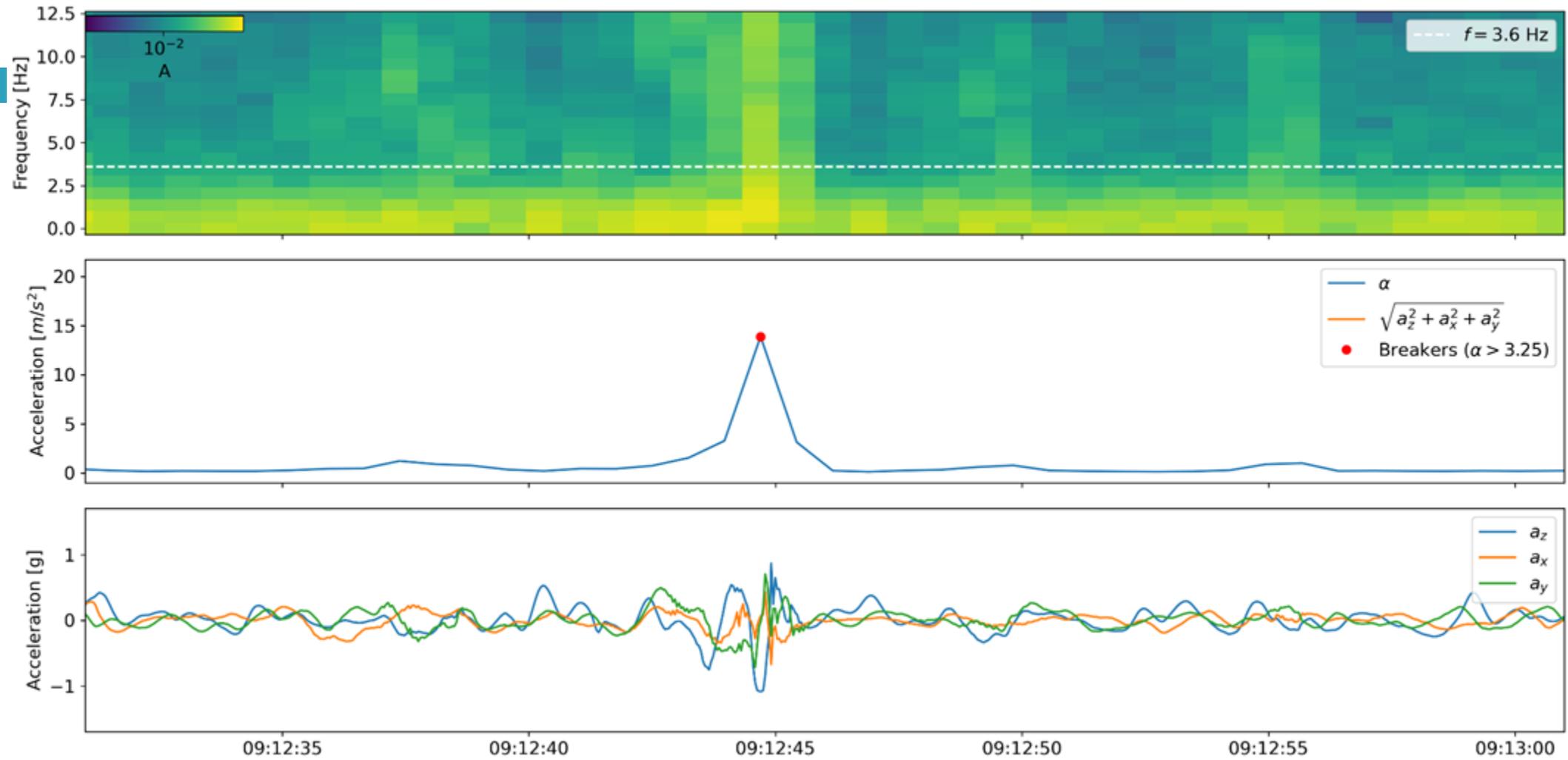


April 2024: Deployment of SFY miniature wave buoys in the stereo camera footprint

- Sample rate: **52 Hz sampling rate**, filtered (FIR) and downsampled from *208 Hz input to AHRS algorithm*.
- Output:
 - Absolute vertical acceleration
 - horizontal acceleration, but not oriented in fixed direction over time
- Batteries:
 - Alkaline C-cells: safer than Lithium in ocean-water.
- Transmits at configured interval, or when memory is full. I.e. every 20 minutes at 52 Hz.
- Telemetry: **Cellular network**, GSM, LTE.
- Georeference and time: GPS/GNSS/GLONASS
- Onboard storage: SD-card
- Cost of parts: **About 2000 NOK / 200 USD.**

Hardware, code and processing: <https://github.com/gauteh/sfy>

SFY: Capable of detecting individual breaking events



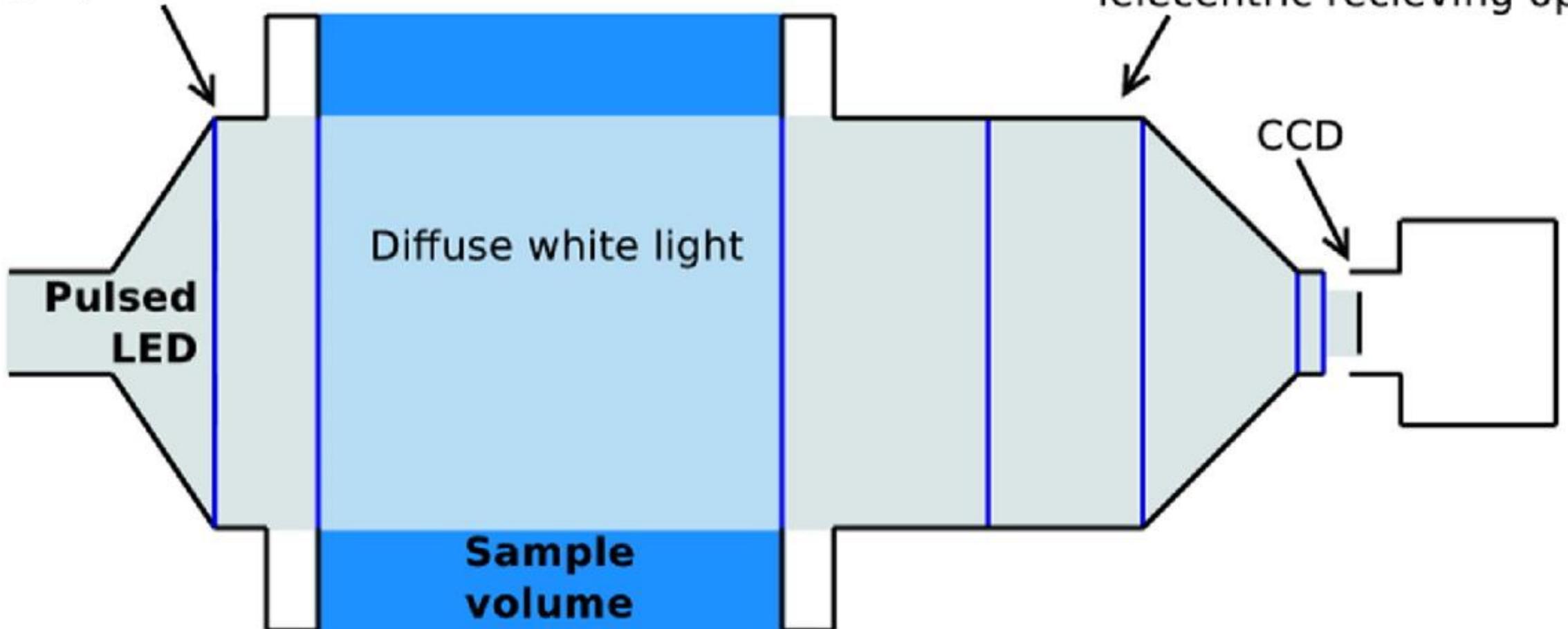
Sintef's Spartacus buoy equipped with telecentric lens for bubble size distribution



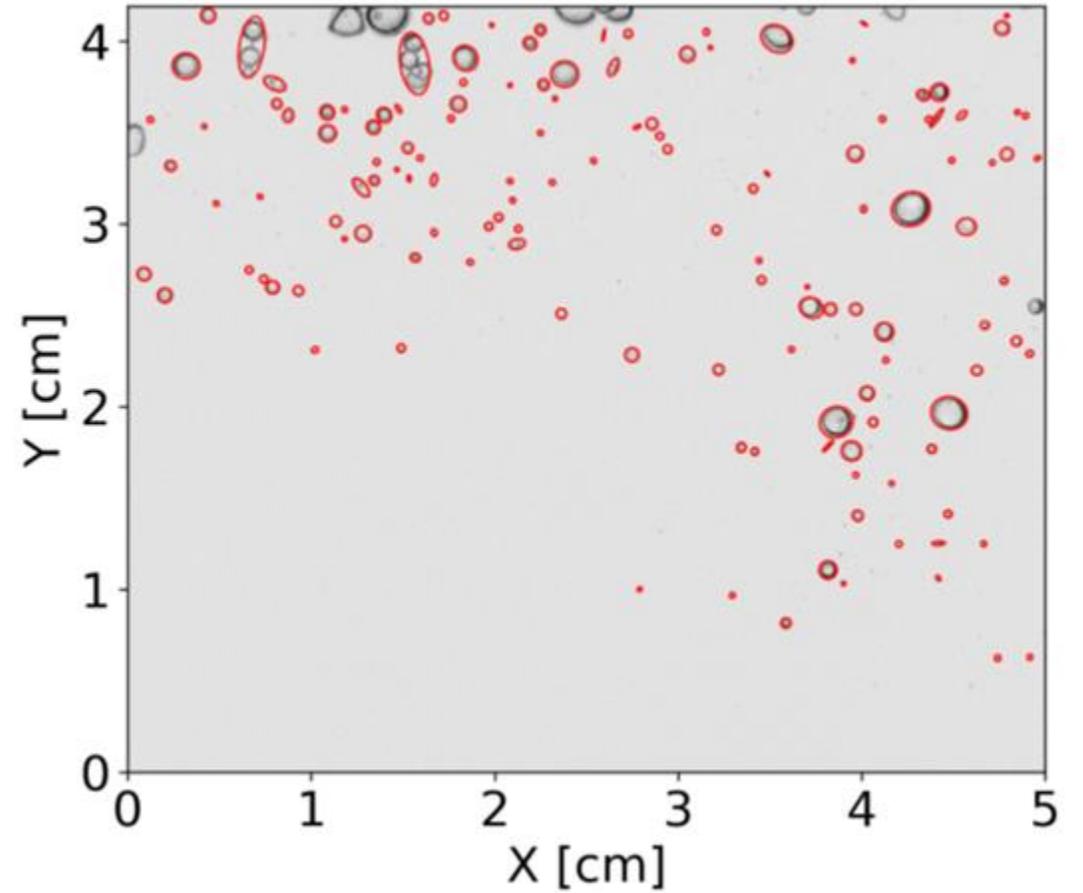
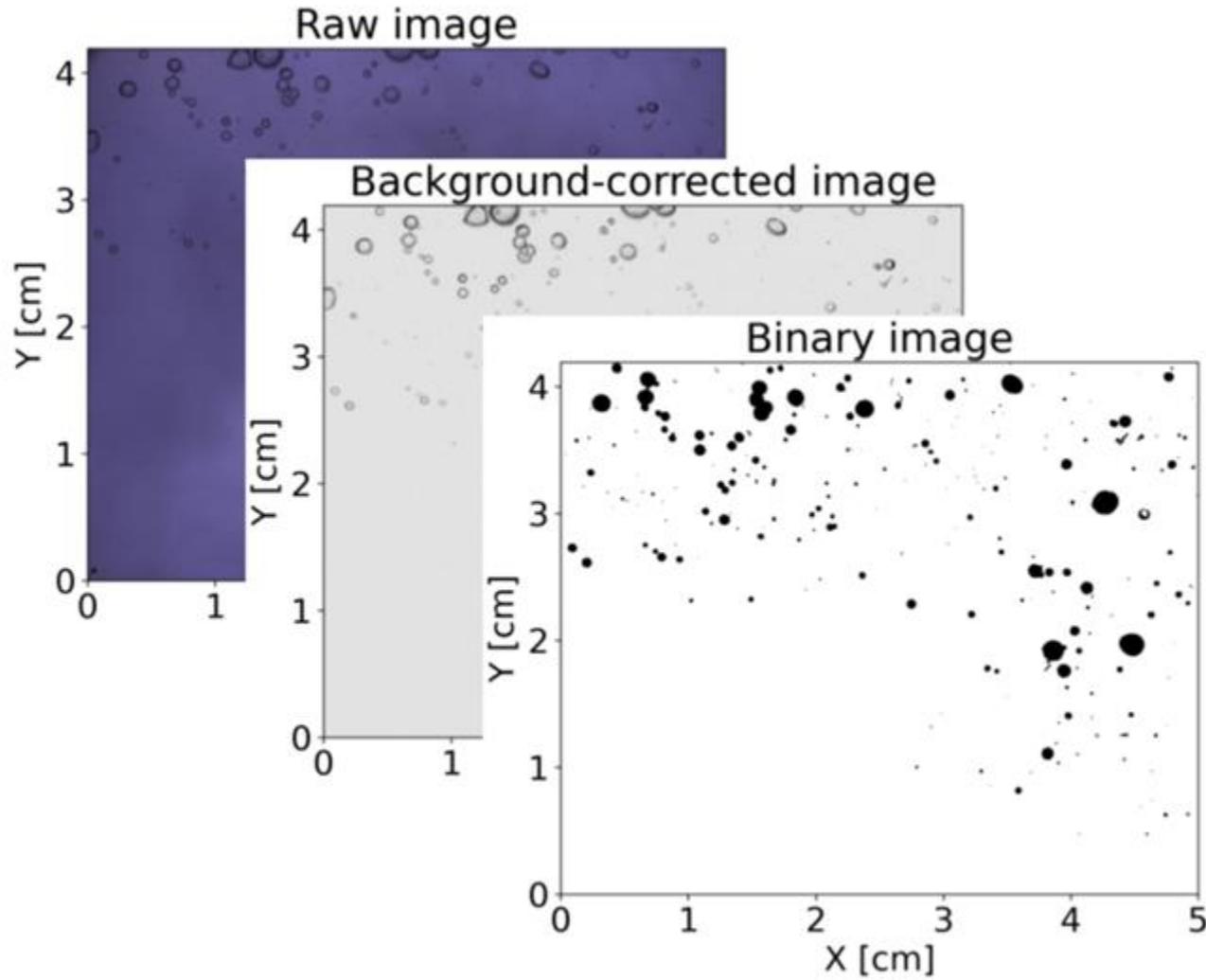
Holographic diffuser



Telecentric receiving optics



From telecentric images to bubble size distribution



Conclusion



The time is ripe.

- We have the components to go and measure the properties postulated to be proportional to the momenta of Phillips' breaking crest length distribution.
- We can now combine new types of instruments in open-ocean conditions and help inform a new generation of wave models,
- but also, even more importantly, the parameterisations that need to go into coupled earth system models.